



## TEST PAPER OF JEE(MAIN) EXAMINATION – 2019

(Held On Wednesday 09<sup>th</sup> JANUARY, 2019) TIME : 02 : 30 PM To 05 : 30 PM

## MATHEMATICS

1. Let  $f$  be a differentiable function from  $\mathbb{R}$  to  $\mathbb{R}$  such that  $|f(x) - f(y)| \leq 2|x - y|^{\frac{3}{2}}$ , for all  $x, y \in \mathbb{R}$ . If

$f(0) = 1$  then  $\int_0^1 f^2(x) dx$  is equal to

- (1) 0      (2)  $\frac{1}{2}$       (3) 2      (4) 1

**Ans. (4)**

**Sol.**  $|f(x) - f(y)| \leq 2|x - y|^{\frac{3}{2}}$

divide both sides by  $|x - y|$

$$\left| \frac{f(x) - f(y)}{x - y} \right| \leq 2|x - y|^{\frac{1}{2}}$$

apply limit  $x \rightarrow y$

$$|f'(y)| \leq 0 \Rightarrow f'(y) = 0 \Rightarrow f(y) = c \Rightarrow f(x) = 1$$

$$\int_0^1 1 \cdot dx = 1$$

2. If  $\int_0^{\frac{\pi}{3}} \frac{\tan \theta}{\sqrt{2k \sec \theta}} d\theta = 1 - \frac{1}{\sqrt{2}}$ , ( $k > 0$ ), then the

value of  $k$  is :

- (1) 2      (2)  $\frac{1}{2}$       (3) 4      (4) 1

**Ans. (1)**

$$\begin{aligned} \text{Sol. } \int_0^{\frac{\pi}{3}} \frac{\tan \theta}{\sqrt{2k \sec \theta}} d\theta &= \frac{1}{\sqrt{2k}} \int_0^{\frac{\pi}{3}} \frac{\sin \theta}{\sqrt{\cos \theta}} d\theta \\ &= -\frac{1}{\sqrt{2k}} 2\sqrt{\cos \theta} \Big|_0^{\frac{\pi}{3}} = -\frac{\sqrt{2}}{\sqrt{k}} \left( \frac{1}{\sqrt{2}} - 1 \right) \end{aligned}$$

$$\text{given it is } 1 - \frac{1}{\sqrt{2}} \Rightarrow k = 2$$

3. The coefficient of  $t^4$  in the expansion of

$$\left( \frac{1-t^6}{1-t} \right)^3 \text{ is}$$

- (1) 12      (2) 15      (3) 10      (4) 14

**Ans. (2)**

$$\text{Sol. } (1 - t^6)^3 (1 - t)^{-3}$$

$$(1 - t^{18} - 3t^6 + 3t^{12}) (1 - t)^{-3}$$

$$\Rightarrow \text{coefficient of } t^4 \text{ in } (1 - t)^{-3} \text{ is}$$

$${}^{3+4-1}C_4 = {}^6C_2 = 15$$

4. For each  $x \in \mathbb{R}$ , let  $[x]$  be the greatest integer less than or equal to  $x$ . Then

$$\lim_{x \rightarrow 0^+} \frac{x([x] + |x|) \sin [x]}{|x|} \text{ is equal to}$$

- (1)  $-\sin 1$       (2) 0      (3) 1      (4)  $\sin 1$

**Ans. (1)**

$$\text{Sol. } \lim_{x \rightarrow 0^+} \frac{x([x] + |x|) \sin [x]}{|x|}$$

$$x \rightarrow 0^+$$

$$[x] = -1 \Rightarrow \lim_{x \rightarrow 0^+} \frac{x(-x-1) \sin(-1)}{-x} = -\sin 1$$

$$|x| = -x$$

5. If both the roots of the quadratic equation  $x^2 - mx + 4 = 0$  are real and distinct and they lie in the interval  $[1, 5]$ , then  $m$  lies in the interval:

- (1) (4, 5)      (2) (3, 4)      (3) (5, 6)      (4)  $(-5, -4)$

**Ans. (Bonus/1)**

$$\text{Sol. } x^2 - mx + 4 = 0$$

$$\alpha, \beta \in [1, 5]$$

$$(1) D > 0 \Rightarrow m^2 - 16 > 0$$

$$\Rightarrow m \in (-\infty, -4) \cup (4, \infty)$$

$$(2) f(1) \geq 0 \Rightarrow 5 - m \geq 0 \Rightarrow m \in (-\infty, 5]$$

$$(3) f(5) \geq 0 \Rightarrow 29 - 5m \geq 0 \Rightarrow m \in \left(-\infty, \frac{29}{5}\right]$$

$$(4) 1 < \frac{-b}{2a} < 5 \Rightarrow 1 < \frac{m}{2} < 5 \Rightarrow m \in (2, 10)$$

$$\Rightarrow m \in (4, 5)$$

No option correct : Bonus

\* If we consider  $\alpha, \beta \in (1, 5)$  then option (1) is correct.


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6. If

$$A = \begin{bmatrix} e^t & e^{-t} \cos t & e^{-t} \sin t \\ e^t & -e^{-t} \cos t - e^{-t} \sin t & -e^{-t} \sin t + e^{-t} \cos t \\ e^t & 2e^{-t} \sin t & -2e^{-t} \cos t \end{bmatrix}$$

Then A is-

- (1) Invertible only if  $t = \frac{\pi}{2}$   
 (2) not invertible for any  $t \in \mathbb{R}$   
 (3) invertible for all  $t \in \mathbb{R}$   
 (4) invertible only if  $t = \pi$

**Ans. (3)**

**Sol.**  $|A| = e^{-t} \begin{vmatrix} 1 & \cos t & \sin t \\ 1 & -\cos t - \sin t & -\sin t + \cos t \\ 1 & 2 \sin t & -2 \cos t \end{vmatrix}$

$$= e^{-t}[5\cos^2 t + 5\sin^2 t] \quad \forall t \in \mathbb{R}$$

$$= 5e^{-t} \neq 0 \quad \forall t \in \mathbb{R}$$

7. The area of the region

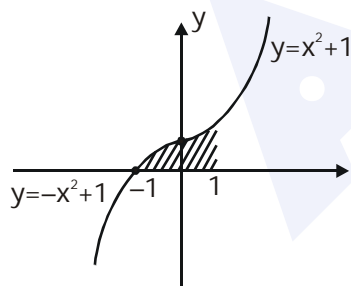
$$A = \{(x, y) : 0 \leq y \leq x|x| + 1 \text{ and } -1 \leq x \leq 1\}$$

in sq. units, is :

- (1)  $\frac{2}{3}$       (2)  $\frac{1}{3}$       (3) 2      (4)  $\frac{4}{3}$

**Ans. (3)**

**Sol.** The graph is as follows



$$\int_{-1}^0 (-x^2 + 1) dx + \int_0^1 (x^2 + 1) dx = 2$$

8. Let  $z_0$  be a root of the quadratic equation,  $x^2 + x + 1 = 0$ . If  $z = 3 + 6iz_0^{81} - 3iz_0^{93}$ , then  $\arg z$  is equal to:

- (1)  $\frac{\pi}{4}$       (2)  $\frac{\pi}{3}$       (3) 0      (4)  $\frac{\pi}{6}$

**Ans. (1)**

**Sol.**  $z_0 = \omega$  or  $\omega^2$  (where  $\omega$  is a non-real cube root of unity)

$$z = 3 + 6i(\omega)^{81} - 3i(\omega)^{93}$$

$$z = 3 + 3i$$

$$\Rightarrow \arg z = \frac{\pi}{4}$$

9. Let  $\vec{a} = \hat{i} + \hat{j} + \sqrt{2}\hat{k}$ ,  $\vec{b} = b_1\hat{i} + b_2\hat{j} + \sqrt{2}\hat{k}$  and  $\vec{c} = 5\hat{i} + \hat{j} + \sqrt{2}\hat{k}$  be three vectors such that the projection vector of  $\vec{b}$  on  $\vec{a}$  is  $\vec{a}$ . If  $\vec{a} + \vec{b}$  is perpendicular to  $\vec{c}$ , then  $|\vec{b}|$  is equal to:

- (1)  $\sqrt{22}$       (2) 4      (3)  $\sqrt{32}$       (4) 6

**Ans. (4)**

**Sol.** Projection of  $\vec{b}$  on  $\vec{a} = \frac{\vec{a} \cdot \vec{b}}{|\vec{a}|} = |\vec{a}|$

$$\Rightarrow b_1 + b_2 = 2 \quad \dots(1)$$

$$\text{and } (\vec{a} + \vec{b}) \perp \vec{c} \Rightarrow (\vec{a} + \vec{b}) \cdot \vec{c} = 0$$

$$\Rightarrow 5b_1 + b_2 = -10 \quad \dots(2)$$

$$\text{from (1) and (2)} \Rightarrow b_1 = -3 \text{ and } b_2 = 5$$

$$\text{then } |\vec{b}| = \sqrt{b_1^2 + b_2^2 + 2} = 6$$

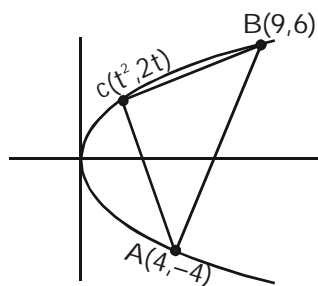
10. Let A(4, -4) and B(9, 6) be points on the parabola,  $y^2 + 4x$ . Let C be chosen on the arc AOB of the parabola, where O is the origin, such that the area of  $\Delta ACB$  is maximum. Then, the area (in sq. units) of  $\Delta ACB$ , is:

- (1)  $31\frac{3}{4}$       (2) 32      (3)  $30\frac{1}{2}$       (4)  $31\frac{1}{4}$

**Ans. (4)**


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Sol.



$$\text{Area} = 5|t^2 - t - 6| = 5\left|\left(t - \frac{1}{2}\right)^2 - \frac{25}{4}\right|$$

is maximum if  $t = \frac{1}{2}$

11. The logical statement

$[\sim(\sim p \vee q) \vee (p \wedge r) \wedge (\sim q \wedge r)]$  is equivalent to:

- (1)  $(p \wedge r) \wedge \sim q$                       (2)  $(\sim p \wedge \sim q) \wedge r$   
 (3)  $\sim p \vee r$                               (4)  $(p \wedge \sim q) \vee r$

Ans. (1)

Sol.  $s[\sim(\sim p \vee q) \wedge (p \wedge r)] \wedge (\sim q \wedge r)$

$$\equiv [(p \wedge \sim q) \vee (p \wedge r)] \wedge (\sim q \wedge r)$$

$$\equiv [p \wedge (\sim q \vee r)] \wedge (\sim q \wedge r)$$

$$\equiv p \wedge (\sim q \wedge r)$$

$$\equiv (p \wedge r) \wedge \sim q$$

12. An urn contains 5 red and 2 green balls. A ball is drawn at random from the urn. If the drawn ball is green, then a red ball is added to the urn and if the drawn ball is red, then a green ball is added to the urn; the original ball is not returned to the urn. Now, a second ball is drawn at random from it. The probability that the second ball is red, is :

- (1)  $\frac{26}{49}$       (2)  $\frac{32}{49}$       (3)  $\frac{27}{49}$       (4)  $\frac{21}{49}$

Ans. (2)

Sol.  $E_1$  : Event of drawing a Red ball and placing a green ball in the bag

$E_2$  : Event of drawing a green ball and placing a red ball in the bag

$E$  : Event of drawing a red ball in second draw

$$P(E) = P(E_1) \times P\left(\frac{E}{E_1}\right) + P(E_2) \times P\left(\frac{E}{E_2}\right)$$

$$= \frac{5}{7} \times \frac{4}{7} + \frac{2}{7} \times \frac{6}{7} = \frac{32}{49}$$

13. If  $0 \leq x < \frac{\pi}{2}$ , then the number of values of  $x$  for which  $\sin x - \sin 2x + \sin 3x = 0$ , is

- (1) 2    (2) 1  
 (3) 3    (4) 4

Ans. (1)

Sol.  $\sin x - \sin 2x + \sin 3x = 0$

$$\Rightarrow (\sin x + \sin 3x) - \sin 2x = 0$$

$$\Rightarrow 2\sin x \cdot \cos x - \sin 2x = 0$$

$$\Rightarrow \sin 2x(2 \cos x - 1) = 0$$

$$\Rightarrow \sin 2x = 0 \text{ or } \cos x = \frac{1}{2}$$

$$\Rightarrow x = 0, \frac{\pi}{3}$$

14. The equation of the plane containing the straight

line  $\frac{x}{2} = \frac{y}{3} = \frac{z}{4}$  and perpendicular to the plane

containing the straight lines

$$\frac{x}{3} = \frac{y}{4} = \frac{z}{2} \text{ and } \frac{x}{4} = \frac{y}{2} = \frac{z}{3} \text{ is:}$$

- (1)  $x + 2y - 2z = 0$                       (2)  $x - 2y + z = 0$   
 (3)  $5x + 2y - 4z = 0$                       (4)  $3x + 2y - 3z = 0$

Ans. (2)



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**Sol.** Vector along the normal to the plane containing the lines

$$\frac{x}{3} = \frac{y}{4} = \frac{z}{2} \quad \text{and} \quad \frac{x}{4} = \frac{y}{2} = \frac{z}{3}$$

$$\text{is } (8\hat{i} - \hat{j} - 10\hat{k})$$

vector perpendicular to the vectors  $2\hat{i} + 3\hat{j} + 4\hat{k}$

and  $8\hat{i} - \hat{j} - 10\hat{k}$  is  $26\hat{i} - 52\hat{j} + 26\hat{k}$

so, required plane is

$$26x - 52y + 26z = 0$$

$$x - 2y + z = 0$$

**15.** Let the equations of two sides of a triangle be  $3x - 2y + 6 = 0$  and  $4x + 5y - 20 = 0$ . If the orthocentre of this triangle is at  $(1,1)$ , then the equation of its third side is :

(1)  $122y - 26x - 1675 = 0$

(2)  $26x + 61y + 1675 = 0$

(3)  $122y + 26x + 1675 = 0$

(4)  $26x - 122y - 1675 = 0$

**Ans. (4)**

**Sol.** Equation of AB is

$$3x - 2y + 6 = 0$$

equation of AC is

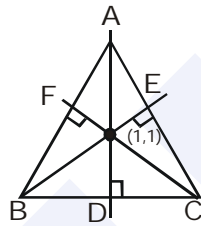
$$4x + 5y - 20 = 0$$

Equation of BE is

$$2x + 3y - 5 = 0$$

Equation of CF is  $5x - 4y - 1 = 0$

$\Rightarrow$  Equation of BC is  $26x - 122y = 1675$



**16.** If  $x = 3 \tan t$  and  $y = 3 \sec t$ , then the value of

$\frac{d^2y}{dx^2}$  at  $t = \frac{\pi}{4}$ , is:

(1)  $\frac{3}{2\sqrt{2}}$     (2)  $\frac{1}{3\sqrt{2}}$     (3)  $\frac{1}{6}$     (4)  $\frac{1}{6\sqrt{2}}$

**Ans. (4)**

**Sol.**  $\frac{dx}{dt} = 3 \sec^2 t$

$$\frac{dy}{dt} = 3 \sec t \tan t$$

$$\frac{dy}{dx} = \frac{\tan t}{\sec t} = \sin t$$

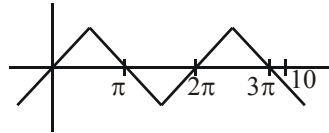
$$\frac{d^2y}{dx^2} = \cos t \frac{dt}{dx}$$

$$= \frac{\cos t}{3 \sec^2 t} = \frac{\cos^3 t}{3} = \frac{1}{3 \cdot 2\sqrt{2}} = \frac{1}{6\sqrt{2}}$$

**17.** If  $x = \sin^{-1}(\sin 10)$  and  $y = \cos^{-1}(\cos 10)$ , then  $y - x$  is equal to:

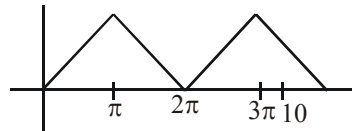
(1)  $\pi$     (2)  $7\pi$     (3)  $0$     (4)  $10$

**Ans. (1)**



**Sol.**

$$x = \sin^{-1}(\sin 10) = 3\pi - 10$$



$$y = \cos^{-1}(\cos 10) = 4\pi - 10$$

$$y - x = \pi$$

**18.** If the lines  $x = ay + b$ ,  $z = cy + d$  and  $x = a'z + b'$ ,  $y = c'z + d'$  are perpendicular, then:

(1)  $cc' + a + a' = 0$

(2)  $aa' + c + c' = 0$

(3)  $ab' + bc' + 1 = 0$

(4)  $bb' + cc' + 1 = 0$

**Ans. (2)**

**Sol.** Line  $x = ay + b$ ,  $z = cy + d \Rightarrow \frac{x-b}{a} = \frac{y}{1} = \frac{z-d}{c}$

Line  $x = a'z + b'$ ,  $y = c'z + d'$

$$\Rightarrow \frac{x-b'}{a'} = \frac{y-d'}{c'} = \frac{z}{1}$$

Given both the lines are perpendicular

$$\Rightarrow aa' + c' + c = 0$$

**19.** The number of all possible positive integral values of  $\alpha$  for which the roots of the quadratic equation,  $6x^2 - 11x + \alpha = 0$  are rational numbers is :

(1) 2    (2) 5    (3) 3    (4) 4

**Ans. (3)**

**Sol.**  $6x^2 - 11x + \alpha = 0$

given roots are rational

$\Rightarrow D$  must be perfect square

$$\Rightarrow 121 - 24\alpha = \lambda^2$$

$\Rightarrow$  maximum value of  $\alpha$  is 5

$$\alpha = 1 \Rightarrow \lambda \notin \mathbb{I}$$

$$\alpha = 2 \Rightarrow \lambda \notin \mathbb{I}$$

$$\alpha = 3 \Rightarrow \lambda \in \mathbb{I}$$

$$\alpha = 4 \Rightarrow \lambda \in \mathbb{I}$$

$$\alpha = 5 \Rightarrow \lambda \in \mathbb{I}$$

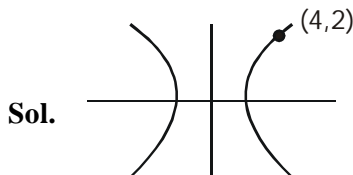
$\Rightarrow$  3 integral values



20. A hyperbola has its centre at the origin, passes through the point (4,2) and has transverse axis of length 4 along the x-axis. Then the eccentricity of the hyperbola is :

- (1)  $\frac{2}{\sqrt{3}}$     (2)  $\frac{3}{2}$     (3)  $\sqrt{3}$     (4) 2

Ans. (1)



$$\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$$

$$2a = 4 \quad a = 2$$

$$\frac{x^2}{4} - \frac{y^2}{b^2} = 1$$

Passes through (4,2)

$$4 - \frac{4}{b^2} = 1 \Rightarrow b^2 = \frac{4}{3} \Rightarrow e = \frac{2}{\sqrt{3}}$$

21. Let  $A = \{x \in \mathbb{R} : x \text{ is not a positive integer}\}$

Define a function  $f : A \rightarrow \mathbb{R}$  as  $f(x) = \frac{2x}{x-1}$  then  $f$  is

- (1) injective but not surjective  
 (2) not injective  
 (3) surjective but not injective  
 (4) neither injective nor surjective

Ans. (1)

Sol.  $f(x) = 2 \left( 1 + \frac{1}{x-1} \right)$

$$f'(x) = -\frac{2}{(x-1)^2}$$

$\Rightarrow f$  is one-one but not onto

22. If  $f(x) = \int \frac{5x^8 + 7x^6}{(x^2 + 1 + 2x^7)^2} dx, (x \geq 0)$  and  $f(0) = 0$ , then the value of  $f(1)$  is :

- (1)  $-\frac{1}{2}$     (2)  $\frac{1}{2}$     (3)  $-\frac{1}{4}$     (4)  $\frac{1}{4}$

Ans. (4)

Sol. 
$$\int \frac{5x^8 + 7x^6}{(x^2 + 1 + 2x^7)^2} dx$$

$$= \int \frac{5x^{-6} + 7x^{-8}}{\left(\frac{1}{x^7} + \frac{1}{x^5} + 2\right)^2} dx = \frac{1}{2 + \frac{1}{x^5} + \frac{1}{x^7}} + C$$

As  $f(0) = 0, f(x) = \frac{x^7}{2x^7 + x^2 + 1}$

$$f(1) = \frac{1}{4}$$

23. If the circles  $x^2 + y^2 - 16x - 20y + 164 = r^2$  and  $(x-4)^2 + (y-7)^2 = 36$  intersect at two distinct points, then:

- (1)  $0 < r < 1$     (2)  $1 < r < 11$   
 (3)  $r > 11$     (4)  $r = 11$

Ans. (2)

Sol.  $x^2 + y^2 - 16x - 20y + 164 = r^2$

$A(8,10), R_1 = r$

$(x-4)^2 + (y-7)^2 = 36$

$B(4,7), R_2 = 6$

$|R_1 - R_2| < AB < R_1 + R_2$

$\Rightarrow 1 < r < 11$

24. Let  $S$  be the set of all triangles in the  $xy$ -plane, each having one vertex at the origin and the other two vertices lie on coordinate axes with integral coordinates. If each triangle in  $S$  has area 50sq. units, then the number of elements in the set  $S$  is:

- (1) 9    (2) 18    (3) 32    (4) 36

Ans. (4)

Sol. Let  $A(\alpha,0)$  and  $B(0,\beta)$

be the vectors of the given triangle  $AOB$

$\Rightarrow |\alpha\beta| = 100$

$\Rightarrow$  Number of triangles

$= 4 \times (\text{number of divisors of } 100)$

$= 4 \times 9 = 36$

25. The sum of the following series

$$1 + 6 + \frac{9(1^2 + 2^2 + 3^2)}{7} + \frac{12(1^2 + 2^2 + 3^2 + 4^2)}{9}$$

$$+ \frac{15(1^2 + 2^2 + \dots + 5^2)}{11} + \dots \text{ up to 15 terms, is:}$$

- (1) 7820    (2) 7830    (3) 7520    (4) 7510

Ans. (1)



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**Sol.**  $T_n = \frac{(3+(n-1) \times 3)(1^2 + 2^2 + \dots + n^2)}{(2n+1)}$

$$T_n = \frac{3 \cdot \frac{n(n+1)(2n+1)}{6}}{2n+1} = \frac{n^2(n+1)}{2}$$

$$S_{15} = \frac{1}{2} \sum_{n=1}^{15} (n^3 + n^2) = \frac{1}{2} \left[ \left( \frac{15(15+1)}{2} \right)^2 + \frac{15 \times 16 \times 31}{6} \right]$$

$$= 7820$$

- 26.** Let a, b and c be the 7<sup>th</sup>, 11<sup>th</sup> and 13<sup>th</sup> terms respectively of a non-constant A.P. If these are also the three consecutive terms of a G.P., then  $\frac{a}{c}$  is equal to:

(1)  $\frac{1}{2}$

(2) 4

(3) 2

(4)  $\frac{7}{13}$

**Ans. (2)**

**Sol.**  $a = A + 6d$

$$b = A + 10d$$

$$c = A + 12d$$

a, b, c are in G.P.

$$\Rightarrow (A + 10d)^2 = (A + 6d)(A + 12d)$$

$$\Rightarrow \frac{A}{d} = -14$$

$$\frac{a}{c} = \frac{A + 6d}{A + 12d} = \frac{6 + \frac{A}{d}}{12 + \frac{A}{d}} = \frac{6 - 14}{12 - 14} = 4$$

- 27.** If the system of linear equations

$$x - 4y + 7z = g$$

$$3y - 5z = h$$

$$-2x + 5y - 9z = k$$

is consistent, then :

(1)  $g + h + k = 0$

(2)  $2g + h + k = 0$

(3)  $g + h + 2k = 0$

(4)  $g + 2h + k = 0$

**Ans. (2)**

**Sol.**  $P_1 \equiv x - 4y + 7z - g = 0$

$$P_2 \equiv 3x - 5y - h = 0$$

$$P_3 \equiv -2x + 5y - 9z - k = 0$$

Here  $\Delta = 0$

$$2P_1 + P_2 + P_3 = 0 \text{ when } 2g + h + k = 0$$

- 28.** Let  $f: [0, 1] \rightarrow \mathbb{R}$  be such that  $f(xy) = f(x)f(y)$  for all  $x, y, \varepsilon [0, 1]$ , and  $f(0) \neq 0$ . If  $y = y(x)$  satisfies the

differential equation,  $\frac{dy}{dx} = f(x)$  with

$$y(0) = 1, \text{ then } y\left(\frac{1}{4}\right) + y\left(\frac{3}{4}\right) \text{ is equal to}$$

(1) 4

(2) 3

(3) 5

(4) 2

**Ans. (2)**

**Sol.**  $f(xy) = f(x) \cdot f(y)$

$$f(0) = 1 \text{ as } f(0) \neq 0$$

$$\Rightarrow f(x) = 1$$

$$\frac{dy}{dx} = f(x) = 1$$

$$\Rightarrow y = x + c$$

$$\text{At, } x = 0, y = 1 \Rightarrow c = 1$$

$$y = x + 1$$

$$\Rightarrow y\left(\frac{1}{4}\right) + y\left(\frac{3}{4}\right) = \frac{1}{4} + 1 + \frac{3}{4} + 1 = 3$$

- 29.** A data consists of n observations:

$$x_1, x_2, \dots, x_n. \text{ If } \sum_{i=1}^n (x_i + 1)^2 = 9n \text{ and}$$

$$\sum_{i=1}^n (x_i - 1)^2 = 5n, \text{ then the standard deviation of}$$

this data is :

(1) 5

(2)  $\sqrt{5}$

(3)  $\sqrt{7}$

(4) 2

**Ans. (2)**





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Sol.  $\sum (x_i + 1)^2 = 9n \quad \dots(1)$

$\sum (x_i - 1)^2 = 5n \quad \dots(2)$

(1) + (2)  $\Rightarrow \sum (x_i^2 + 1) = 7n$

$\Rightarrow \frac{\sum x_i^2}{n} = 6$

(1) - (2)  $\Rightarrow 4\sum x_i = 4n$

$\Rightarrow \sum x_i = n$

$\Rightarrow \frac{\sum x_i}{n} = 1$

$\Rightarrow \text{variance} = 6 - 1 = 5$

$\Rightarrow \text{Standard deviation} = \sqrt{5}$

30. The number of natural numbers less than 7,000 which can be formed by using the digits 0,1,3,7,9 (repetition of digits allowed) is equal to :

- (1) 250      (2) 374      (3) 372      (4) 375

Ans. (2)

Sol. 

$a_1$	$a_2$	$a_3$
-------	-------	-------

Number of numbers =  $5^3 - 1$

$a_4$	$a_1$	$a_2$	$a_3$
-------	-------	-------	-------

2 ways for  $a_4$

Number of numbers =  $2 \times 5^3$

Required number =  $5^3 + 2 \times 5^3 - 1$   
= 374

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